

## **Photorealism**

- **Ray Tracing**
- **Texture Mapping**
- **Radiosity**

## **Photorealism -- Taking into Account Global Illumination**

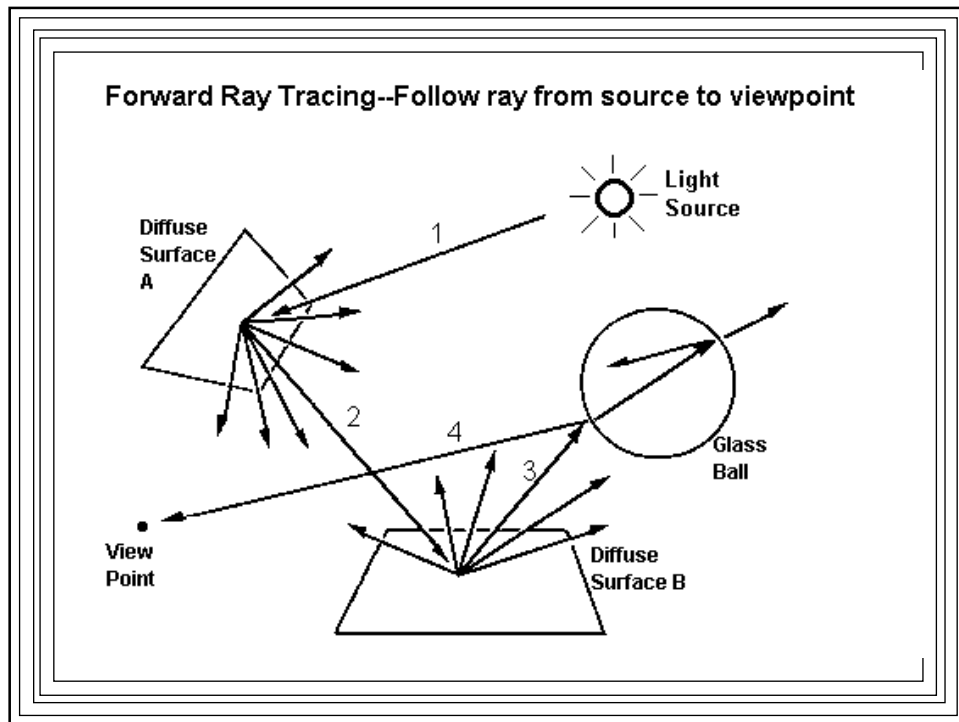
- Light can arrive at surfaces indirectly
- This light called global illumination
- To now we've approximated it with a constant, diffuse ambient term
  - This is wrong
- Need to take into account all the multiply reflected light in the scene
- Two different approaches:
  - Ray Tracing -- specularly reflected light
  - Radiosity -- diffusely reflected light

## Photorealism: Ray Tracing

- See CS-460/560 Notes at:  
<http://www.cs.binghamton.edu/~reckert/460/raytrace.htm>  
<http://www.cs.binghamton.edu/~reckert/460/texture.htm>
- Persistence of Vision Ray Tracer (free):  
<http://povray.org/>

## Ray Tracing

- What is seen by viewer depends on:
  - rays of light that arrive at his/her eye
- So to get “correct” results:
  - Follow all rays of light from all light sources
  - Each time one hits an object, compute the reflected color/intensity
  - Store results for those that go through projection plane pixels into observer’s eye
  - Paint each pixel in the resulting color



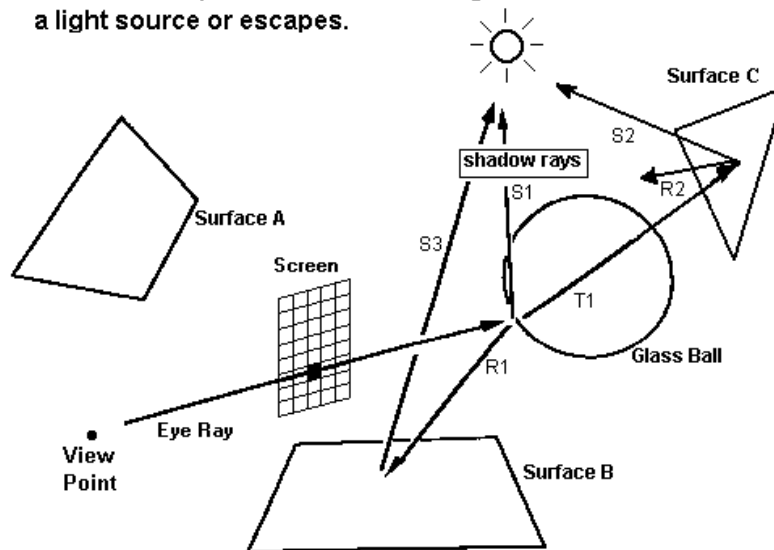
## Forward Ray Tracing

- Infinite number of rays from each source
- At each intersection with an object
  - could have an infinite number of reflected rays
- Completely intractable
- Would take geological times to compute

# Backward Ray Tracing

- Look only at rays observer sees
- Follow rays backwards from eye point through pixels on screen
  - “Eye” rays
- Check if they intersect objects
  - If so, can intersection point see a light source?
    - If so, compute intensity of reflected light
    - If not, point is in the shadow
  - If object has reflectivity/transparency
    - Follow reflected/transmission rays
    - Treat these rays as “eye” rays
    - So it's a recursive algorithm

Backward Ray Tracing--Follow Ray from Eye of viewer and determine its path backwards through the scene until it hits a light source or escapes.



# Recursive Ray Tracing Algorithm

depth = 0

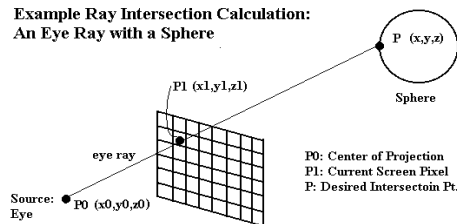
for each pixel (x,y)

Calculate direction from eyepoint to pixel

TraceRay (eyepoint, direction, depth, \*color)

FrameBuf [x,y] = color

Example Ray Intersection Calculation:  
An Eye Ray with a Sphere



TraceRay (start\_pt, direction\_vector, recur\_depth, \*color)

if (recur\_depth > MAXDEPTH) color = Background\_color

else

// Intersect ray with all objects

// Find int. point that is closest to start\_point

// Hidden surface removal is built in

if (no intersection) color = Background\_color

else

// Send out shadow rays toward light sources

if (no intersection with other objects)

local\_color = contribution of illumination model at int. pt.

// Shadows built in

// Calculate direction of reflection ray

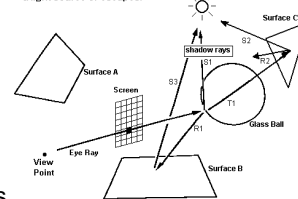
TraceRay (int\_pt, refl\_dir., depth+1, \*refl\_color)

// Calculate direction of transmitted ray

TraceRay (int\_pt., trans\_dir., depth+1, \*trans\_color)

color = Combine (local\_color, refl\_color, trans\_color)

Backward Ray Tracing—Follow Ray from Eye of viewer and determine its path backwards through the scene until it hits a light source or escapes.



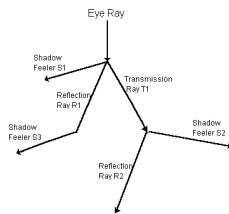
## Combining Color from Reflection Ray

- Add attenuated reflected color intensity to local color intensity:

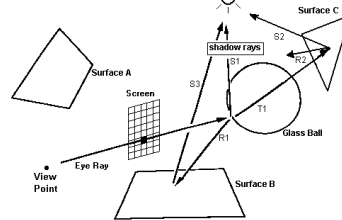
$$\text{color} = \text{local\_color} + k * \text{refl\_color}$$

- here  $\text{refl\_color}$  is  $I(r,g,b)$  - color returned by reflection ray
- $\text{local\_color}$  is  $I(r,g,b)$  - color computed by illumination model at intersection point
- $k$  is an attenuation factor ( $<1$ )

The Ray Tree for the above Scene



Backward Ray Tracing--Follow Ray from Eye of viewer and determine its path backwards through the scene until it hits a light source or escapes.



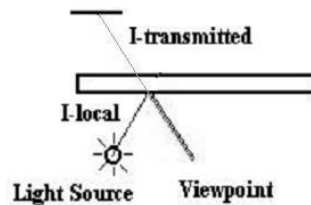
## Combining Color from Transmission Ray

- Observer sees a mixture of light reflected off surface and light transmitted through surface
- So combine colors (interpolate)

$$I(r,g,b) = k' * I_{\text{local}}(r,g,b) + (1 - k') * I_{\text{transmitted}}(r,g,b)$$

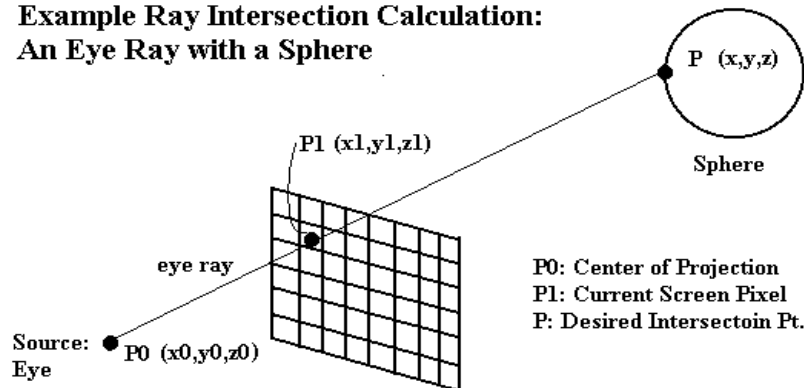
$k'$  is opacity factor coefficient

$k'=0 \Rightarrow$  perfectly transparent,  $k'=1 \Rightarrow$  perfectly opaque



# Ray Tracing Intersection Calculations

**Example Ray Intersection Calculation:  
An Eye Ray with a Sphere**



## Parametric Equations for Eye Ray:

$$x = x_0 + (x_1 - x_0) * t$$

$$x = x_0 + \Delta x * t$$

$$y = y_0 + (y_1 - y_0) * t$$

$$y = y_0 + \Delta y * t$$

$$z = z_0 + (z_1 - z_0) * t$$

$$z = z_0 + \Delta z * t$$

## Equation of a sphere of radius $r$ , centered at $(a,b,c)$

$$(x-a)^2 + (y-b)^2 + (z-c)^2 = r^2$$

Substitute ray parametric equations:

$$(x_0+\Delta x*t-a)^2 + (y_0+\Delta y*t-b)^2 + (z_0+\Delta z*t-c)^2 = r^2$$

Rearrange terms:

$$(\Delta x^2+\Delta y^2+\Delta z^2)t^2 + 2[\Delta x(x_0-a)+\Delta y(y_0-b)+\Delta z(z_0-c)]t + (x_0-a)^2 + (y_0-b)^2 + (z_0-c)^2 - r^2 = 0$$

A quadratic in  $t$ , use quadratic formula to solve for  $t$

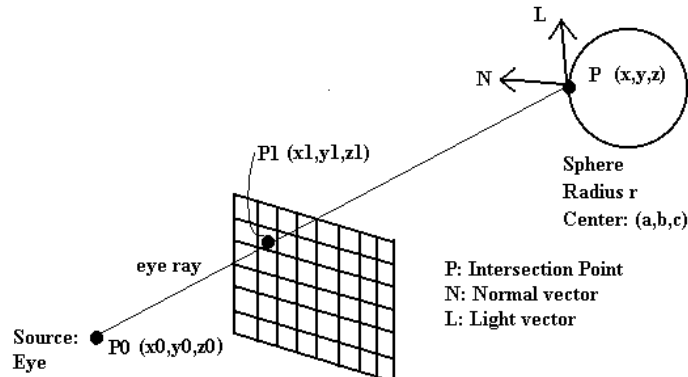
## This is a quadratic in parameter $t$

- Solution(s): value(s) of  $t$  where ray intersects sphere
- Three cases
  - No real roots  $\implies$  no intersection point
  - 1 real root  $\implies$  ray grazes sphere
  - 2 real roots  $\implies$  ray passes thru sphere
    - Select smaller  $t$  (closer to source)



## Sphere Normal Computation

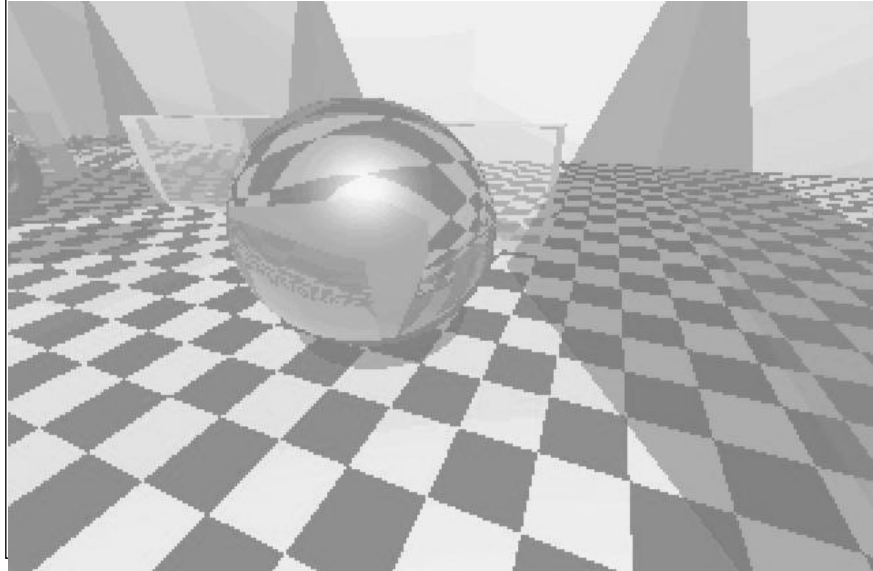
- To apply illumination model at intersection point P, need surface normal
- Can show:  $N = ( (x-a)/r, (y-b)/r, (z-c)/r )$



## Intersections with other Objects

- Handled in similar fashion
- May be difficult to come up with equations for their surfaces
- Sometimes approximation methods must be used to compute intersections of rays with surfaces

## A Ray-Traced Image



## Disadvantages of Ray Tracing

- Computationally intensive
  - But there are several acceleration techniques
- Bad for scenes with lots of diffuse reflection
  - But can be combined with other algorithms that handle diffuse reflection well
- Prone to aliasing
  - One sample per pixel
    - can give ugly artifacts
  - But there are anti-aliasing techniques

## **Persistence of Vision Ray Tracer**

- POVRay free software
- Lots of capabilities
- Great for playing around with ray tracing
  - <http://povray.org/>

## **An Algorithm Animation of a Ray Tracer**

Ray Tracing Algorithm Animator in VC++  
(with David Goldman)

See:

[http://www.cs.binghamton.edu/~reckert/3daape\\_paper.htm](http://www.cs.binghamton.edu/~reckert/3daape_paper.htm)

Ray Tracing Algorithm Animation Java  
Applet and Paper (with Brian Maltzan)

See:

<http://www.cs.binghamton.edu/~reckert/brian/index.html>

## **Pattern/Texture Mapping**

- Adding details or features to surfaces
  - (variations in color or texture)

## **General Texture Mapping**

- Pattern Mapping Technique
  - Modulate surface color calculated by reflection model according to a pattern defined by a texture function
    - (“wrap” pattern around surface)
    - Most common: a 2-D Texture function:  $T(u,v)$ 
      - Define in a 2-D texture space  $(u,v)$
      - Could be a digitized image
      - Or a procedurally-defined pattern

# Inverse Pixel Mapping (Screen Scanning)

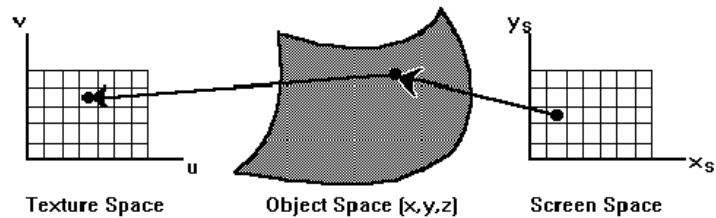
For each pixel on screen ( $x_s, y_s$ )

Compute pt ( $x, y, z$ ) on closest surface projecting to pixel  
(e.g., ray tracing)

Determine color (e.g., apply illumination/reflection model)

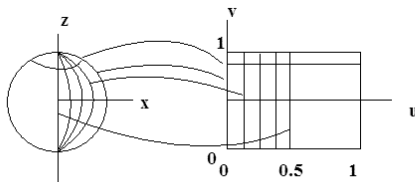
Compute ( $u, v$ ) corresponding to ( $x, y, z$ ) (inverse mapping)

Modulate color of ( $x_s, y_s$ ) according to value of  $T(u, v)$  at ( $u, v$ )



# Inverse Mapping a Sphere

- Lines of longitude: constant  $u$ , corresponds to  $\theta$
- Lines of latitude: constant  $v$ , corresponds to  $\phi$

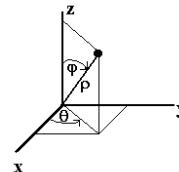


$$\begin{aligned} x &= R \sin(\phi) \cos(\theta) \\ y &= R \sin(\phi) \sin(\theta) \\ z &= R \cos(\phi) \end{aligned}$$

$$\begin{aligned} \phi &= \arccos(z/R) = \arccos(N \cdot z) \\ \theta &= \arccos(x/R \sin(\phi)) \\ \theta &= (\arccos(N \cdot x / \sin(\phi))) \end{aligned}$$

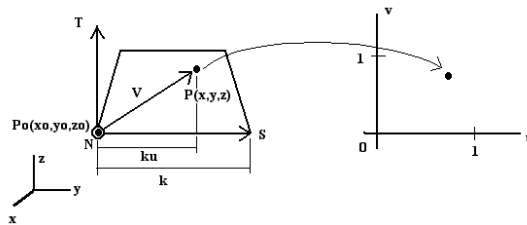
$$v = (\pi - \phi) / \pi \quad \begin{array}{l} \phi=0, \text{ North Pole, } v=1 \\ \phi=\pi, \text{ South Pole, } v=0 \end{array}$$

$$\begin{aligned} u &= \theta / 2\pi \text{ if } N \cdot y \text{ is } + & \theta=0, u=0; \theta=\pi, u=0.5 & \text{ (+y side)} \\ u &= 1 - \theta / 2\pi \text{ if } N \cdot y \text{ is } - & \theta=\pi, u=0.5; \theta=0, u=1.0 & \text{ (-y side)} \end{aligned}$$

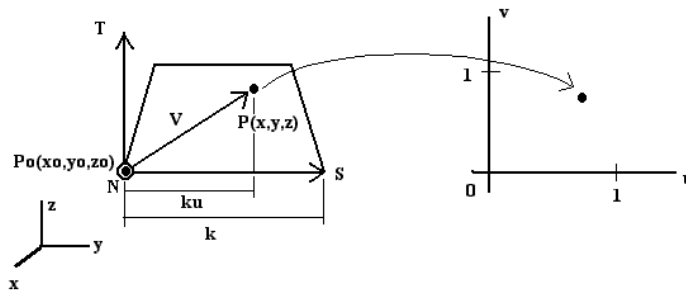


## Ex: Inverse Mapping a Polygon

- Choose axis  $S$  (unit vector) along a polygon edge
  - will align with  $u$ -axis in texture space
- Choose a polygon vertex  $P_0(x_0, y_0, z_0)$ 
  - will correspond to origin in texture space
- Choose a scaling factor  $k$ 
  - $k = \text{max dimension of polygon}$ 
    - $0-k$  in object space  $\rightarrow 0-1$  in texture space
- Want to map point  $P(x, y, z)$  on polygon to  $(u, v)$



- Construct vector  $V = P - P_0$
- $V \cdot S = k \cdot u$ , projection of  $P$  onto  $S$
- So  $u = V \cdot S / k$
- Choose orthogonal axis  $T$  in polygon plane ( $T = N \times S$ )
- $v = V \cdot T / k$



## **There are lots of other Texture Mapping Techniques**

See Section 10-17 of text book

OpenGL also has extensive support for  
texture mapping

See Section 10-21 of text book

## **Radiosity Methods**

- Alternative to ray tracing for handling global illumination
- Two kinds of illumination at each reflective surface
  - Local: from point sources
  - Global: light reflected from other surfaces in scene (multiple reflections)
  - Ray tracing handles specularly reflected global illumination
    - But not diffusely reflected global illumination

## Radiosity Approach

- Compute global illumination
- All light energy coming off a surface is the sum of:
  - Light emitted by the surface
  - Light from other surfaces reflected off the surface
  - Divide scene into patches that are perfect diffuse reflectors...
    - Reflected light is non-directional
  - and/or emitters

## Definitions

- Radiosity (B):
  - Total light energy per unit area leaving a surface patch per unit time--sum of emitted and reflected energy (Brightness)
- Emission (E):
  - Energy per unit area emitted by the surface itself per unit time (Surfaces having nonzero E are light sources)



- Reflectivity ( $\rho$ ):

- Fraction of light reflected from a surface (a number between 0 and 1)

- Form Factor ( $F_{ij}$ ):

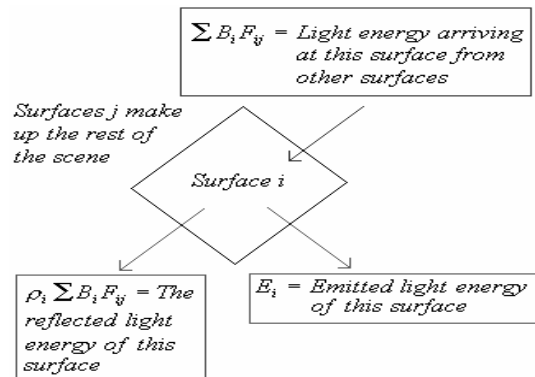
- Fraction of light energy leaving patch i which arrives at patch j
  - Function only of geometry of the environment

- Conservation of energy for patch i:

- Total energy out = Energy emitted + Sum of energy from other patches reflected by patch i:

$$B_i \cdot A_i = E_i \cdot A_i + \rho_i \cdot \sum_j B_j \cdot A_j \cdot F_{ji}$$

$$B_i = E_i + \rho_i \cdot \sum_j (B_j \cdot A_j / A_i) \cdot F_{ji}$$



## ● Principle of Reciprocity for Form Factors

– Reversing role of emitters and receivers:

- Fraction of energy emitted by one and received by other would be same as fraction of energy going the other way

$$\bullet F_{ij} \cdot A_i = F_{ji} \cdot A_j \implies F_{ji} = (A_i/A_j) F_{ij}$$

• So:

$$B_i = E_i + \rho_i \cdot \sum B_j \cdot F_{ij}$$

$$B_i - \rho_i \cdot \sum B_j \cdot F_{ij} = E_i$$

- Need to solve this system of equations for the radiosities  $B_i$

## Radiosity -- Matrix Formulation and Solution

Assume  $N$  patches

$F_{ii} = 0$  – Patch  $i$  receives no energy from itself

Rearranging and writing out the Radiosity equation:

$$\begin{bmatrix} 1 & -\rho_1 F_{12} & -\rho_1 F_{13} & \dots & -\rho_1 F_{1N} \\ -\rho_2 F_{21} & 1 & -\rho_2 F_{23} & \dots & -\rho_2 F_{2N} \\ \dots & \dots & \dots & \dots & \dots \\ -\rho_N F_{N1} & -\rho_N F_{N2} & -\rho_N F_{N3} & \dots & 1 \end{bmatrix} \begin{bmatrix} B_1 \\ B_2 \\ \dots \\ B_N \end{bmatrix} = \begin{bmatrix} E_1 \\ E_2 \\ \dots \\ E_N \end{bmatrix}$$

This is the matrix equation:  $M B = E$

The  $E_i$  and  $\rho_i$  are known, and the form factors  $F_{ij}$  can be calculated so that the matrix elements  $M_{ij}$  can be determined. Since the  $\rho_i$  and  $F_{ij}$  are all less than or equal to one, matrix  $M$  is diagonally dominant, so the Gauss-Seidel iteration method is guaranteed to converge after a few iterations.

# Gauss-Seidel Solution

$$B_1 + M_{12}B_2 + \dots + M_{1N}B_N = E_1$$

$$M_{21}B_1 + B_2 + \dots + M_{2N}B_N = E_2$$

---


$$M_{i1} B_1 + M_{i2} B_2 + \dots + B_i + \dots + M_{iN} B_N = E_i$$


---

Initial guess:  $B_i^{(0)} = E_i$

Next iteration  $B_i^{(1)} = E_i - (M_{i1}B_1^{(0)} + \dots + M_{i,i-1}B_{i-1}^{(0)} + \dots + M_{i,i+1}B_{i+1}^{(0)} + \dots + M_{iN}B_N^{(0)})$

Continue iterating until all the difference between  $B_i^{(k+1)}$  and  $B_i^{(k)}$  is small enough for all patches

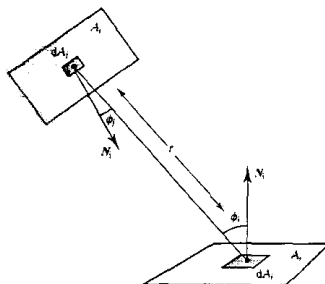
Notice that for each patch  $i$  we are "gathering" radiosity from all the other patches

Thus the scene is not finished until we have processed all patches--very time consuming.

**Problem: getting form factors**

# Computing Form Factors

## Form Factor Determination



The form factor  $F_{ij}$  from patch  $i$  to patch  $j$  is obtained in principle by integrating over both patches:

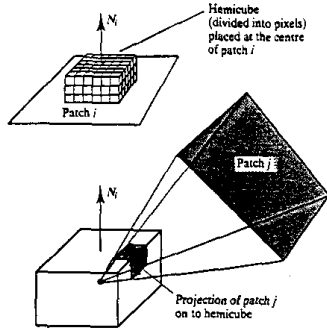
$$F_{A_i A_j} = F_{j i} = \frac{1}{A_i A_j} \int \int \frac{\cos \phi_i \cos \phi_j}{\pi r^2} dA_j dA_i$$

But this is very difficult.

$$\Delta FF = \Sigma (\cos \phi_i \cos \phi_j \Delta A_j) / (\pi r^2), \text{ approximately}$$

# Hemicube Approximation

## The Hemicube Approximation



Calculate and store the delta form factors for each element of the hemicube.

$$F_{ij} = \sum_q \Delta F_q$$

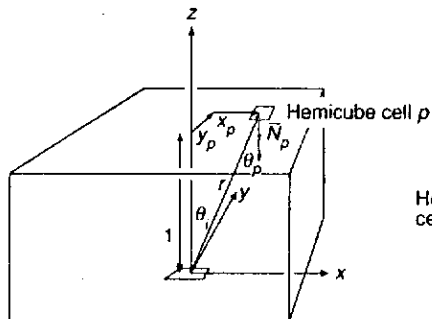
To calculate the form factor  $F_{ij}$ , build a hemicube centered on patch  $i$  and sum the delta form factors for those elements of the hemicube to which patch  $j$  projects.

# Hemicube Pixel Computations

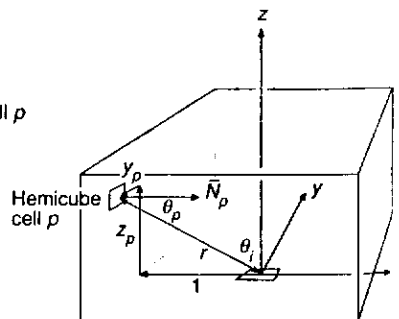
$$\Delta F = \cos\theta_i \cdot \cos\theta_p \cdot \Delta A / (\pi \cdot r^2)$$

a. (top)  $\Delta F = \Delta A / [\pi \cdot (x^2 + y^2 + 1)^2]$

b. (sides)  $\Delta F = z \cdot \Delta A / [\pi \cdot (y^2 + z^2 + 1)^2]$



(a)



(b)

## Hemicube Form Factor Algorithm

Compute & store all hemicube Delta-Form-Factors:  $\Delta FF[k]$

Zero all the Form Factors:  $F_{ij}$

For each patch  $i$

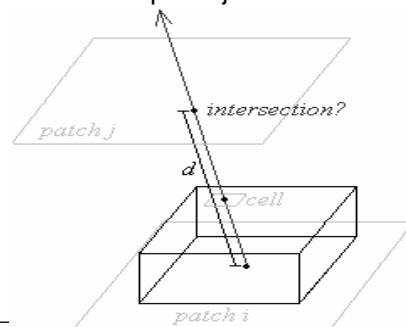
Place a unit hemicube at center of patch  $i$

For each patch  $j$  ( $j \neq i$ )

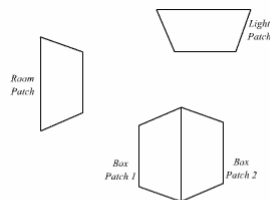
For each cell  $k$  on hemicube

If line from origin through cell  $k$  intersects patch  $j$  & it is closest

$F_{ij} = F_{ij} + \Delta FF[k]$



## Video of Radiosity Form Factor Computation



Here are four patches from various parts of the scene.

Total Form Factors

Room to Light:

Room to Box 1:

Room to Box 2:

## Steps in Applying Radiosity Method

*Summary of Steps:*

*Define a scene.*

*Divide scene into distinct patches.*

*Build a hemicube on each patch and calculate the delta form factors for cell on every hemicube.*

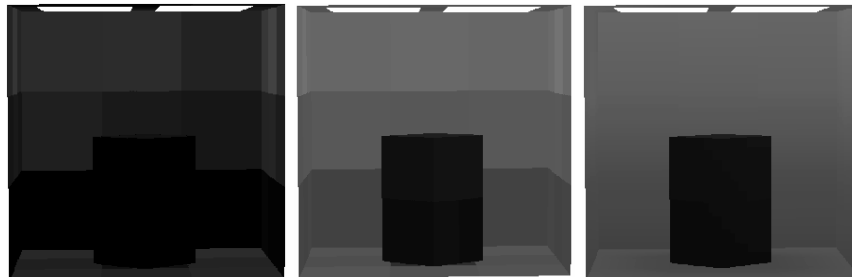
*Calculate a form factor for every pair of patches in the scene.*

*Calculate the red, green, and blue radiosities for each patch.*

*Map all radiosity values to a 0 - 255 color scale.*

*Apply Gouraud shading.*

## Three Simple Radiosity Images



After 1<sup>st</sup> Gauss-Seidel Iteration

No Gouraud Shading

Gouraud Shading

## Radiosity Summary

- Good for scenes with lots of diffuse reflection
- Not good for scenes with lots of specular reflection
  - Complementary to Ray Tracing
  - But can be combined with Ray Tracing
- Very computationally intensive
  - Can take very long times for complex scenes
    - but once patch intensities are computed, scene “walkthroughs” are fast
  - Gauss-Seidel is very memory intensive
  - There are other approaches
    - Progressive Refinement